

# Social Experiments

Handbook of Econometrics

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# 1 Social Experiments

## 1.1 Introduction

Consider ideal experiments with no compliance or attrition problems.

Two distinct cases for the application of the method of randomized trials.

First case advocates randomization to identify structural parameters.

Second and more recent case seeks to use randomization to identify treatment parameters.

## 1.2 Treatment Effects vs. Structural Parameters

Marschak (1953): goal of structural estimation is to solve a variety of decision problems.<sup>1</sup>

Decision problems

- (a) evaluating the effectiveness of an existing policy,
- (b) projecting the effectiveness of a policy to different environments from the one where it was experienced,
- (c) forecasting the effects of a new policy, never previously experienced.

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<sup>1</sup>Recall the opening sentence of his seminal article: “Knowledge is useful if it helps us make the best decisions”. (Marschak, 1953, p.1).

Marschak (1953) realized that for certain decision problems, knowledge of individual structural parameters, or any structural parameter, is unnecessary. Second, and neglected, contribution of his paper, notion of decision-specific parameters.

Prototypical problem of determining the impact of taxes on labor supply  $h$ .

Interior solution labor supply equation of hours of work  $h$ , wages,  $W$ , other variables including assets,  $\varepsilon$  denote an unobservable.

(3-1)

$$h = h(W, X, \varepsilon).$$

Additively separable version of the Marshallian causal function

(3-2)

$$h = h(W, X) + \varepsilon.$$

*ceteris paribus* effects of  $W$  and  $X$  on  $h$

(3-1a)

$$h = h(W, X, \varepsilon, \theta)$$

$\theta$  is a low dimensional parameter that generates  $h$ . Separable version:

(3-2a)

$$h = h(W, X, \theta) + \varepsilon.$$

a linear-in-parameters Cowles Commission type representation of  $h$  :

(3-3)

$$h = \alpha'X + \beta \ln W + \varepsilon$$

Distinguish 3 cases.

(1) The case where tax  $t$  has been implemented in the past and we wish to forecast the effects of the tax in the future in a population with the same distribution of  $(X, \varepsilon)$  variables as prevailed when measurements of tax variation were made.

(2) A second case where tax  $t$  has been implemented in the past but we wish to project the effects of the same tax to a different population of  $(X, \varepsilon)$  variables.

(3) A case where the tax has never been implemented and we wish to forecast the effect of a tax either on an initial population used to estimate (1) or on a different population.

Suppose the goal of the analysis is to determine the effect of taxes on average labor supply on a relevant population with distribution  $G(W, X, \varepsilon)$ .

### **Case One**

Case one, we have data from the same population for which we wish to construct a forecast.

In the randomized trial, persons face tax rate

$$\Pr(T = t_j \mid X, W, \varepsilon) = \Pr(T = t_j \mid X, W).$$



From each regime we can identify

(3-4)

$$E(h | W, X, t_j) = \int h(W(1 - t_j), X, \varepsilon) dG(\varepsilon | X, W, t_j).$$

For the entire population:

(3-4a)

$$E(h | t_j) = \int h(W(1 - t_j), X, \varepsilon) dG(\varepsilon, X, W | t_j).$$

Knowledge of (3-4) or (3-4a) from the historical data. No knowledge of any Marshallian causal function or structural parameter is required to do policy analysis for case one.

## Case Two

Two resembles case one except for one crucial difference. Projecting the same policy onto a different population, it is necessary to break (3-4) or (3-4a) into its components and determine  $h(W(1-t_j), X, \varepsilon)$  separately from  $G(\varepsilon, X, W, t)$ .

## Assumptions Required to Project

(1) Knowledge of  $h(\cdot)$  is needed on the new population. May entail determination of  $h$  on a different support from that used to determine  $h$  in the target population. Structural estimation comes into its own.

Parametric structure (3-3)

Knowledge of  $G(\cdot)$  for the target population is also required. Exogeneity enters, a crucial facilitating assumption.

$$(A-1) (X, W, T) \perp\!\!\!\perp \varepsilon$$

$$G(\varepsilon | X, W, T) = G(\varepsilon).^2$$

Distribution of unobservables is the same in the sample as in the forecast or target regime,  $G(\varepsilon) = G'(\varepsilon)$ ,  $G'(\varepsilon)$  is the distribution of unobservables in the

$$E(h | W, X, t_j) = \int h(W(1 - t_j), X, \varepsilon) dG(\varepsilon)$$

Can determine  $h(\cdot)$  over the new support of  $X$ . If  $G' \neq G$ . Face a new problem.

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<sup>2</sup>There are many definitions of this term. Assumption (A-1) is often supplemented by the additional assumption that the distribution of  $X$  does not depend on the parameters of the model (e.g.  $\theta$  in (2') or (1')).

## Case Three

Third case, knowledge of the target population. Taxes operate through the term  $W(1 - t)$ . No wage variation in samples

If wages vary in the presample period, the support of  $W(1 - t) \stackrel{\text{def}}{=} W^*$  in the target regime is contained in the support of  $W$  in the historical regime, conditional distributions of  $W^*$  and  $W$  given  $X, \varepsilon$  are the same, supports of  $(X, \varepsilon)$  are the same in both regimes,

(a)  $\text{Support } (W^*)_{\text{target}} \subseteq \text{Support } (W)_{\text{historical}}$

(b)  $G(w^* | X, \varepsilon)_{\text{target}} = G(w | X, \varepsilon)_{\text{historical}}$

(c)  $\text{Support } (X, \varepsilon)_{\text{target}} = \text{Support } (X, \varepsilon)_{\text{historical}}$

$$W^* = W(1 - t)$$

Under (a), can find a counterpart value of  $W(1 - t) = W^*$  in the target population. If these conditions are not met, necessary to build up the  $G$  and the  $h$  functions over the new supports using the appropriate distributions. Enter the realm where structural estimation is required.

## 1.3 Two Different Cases For Social Experiments

Demonstrate the contrasting nature of the two cases for social experiments.

Present a form of experimentation that identifies first, historically older, case

seeks to use randomization to identify Marshallian causal functions

“Treatment” is a tax policy: proportional tax on wages.<sup>3</sup>

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<sup>3</sup>Historically, randomization was first used in economics to vary wage and income parameters facing individuals in order to estimate wage and income effects in labor supply to examine the implications of negative income taxes on labor supply. Part of the goal of randomization was to produce variation in wages and incomes to determine estimates of income and substitution effects. See Cain and Watts (1973). Ashenfelter (1983) shows how estimates of income and substitution effects can be used to estimate the impact of negative income taxes on labor supply.

Determine how labor supply responds to taxes  $t$  in an experimentally determined population.

Labor supply equation is  $h = h(t, W, X, \varepsilon)$ , taxes  $T$  are assigned to persons so that

$$(A-5) (T \perp\!\!\!\perp \varepsilon) \parallel (W, X).$$



Thus  $\Pr(T = t \mid W, X, \varepsilon) = \Pr(T = t \mid W, X)$ . Assuming full compliance compute the labor supply given  $t$  (“treatment” or taxes) as

$$E(h \mid t, W, X) = \int h(t, W, X, \varepsilon) dG(\varepsilon \mid t, W, X) = \int h(t, W, X, \varepsilon) dG(\varepsilon \mid W, X)$$

For tax rate  $t'$ ,

$$E(h \mid t', W, X) = \int h(t', W, X, \varepsilon) dG(\varepsilon \mid W, X).$$

Form contrast:

$$E(h | t, W, X) - E(h | t', W, X) = \int [h(t, W, X, \varepsilon) - h(t', W, X, \varepsilon)] dG(\varepsilon | W, X).$$

May remove the conditioning on  $(W, X)$  by integrating out  $(W, X)$  Population average treatment effect for taxes  $(t, t')$  is

$$E_{F_c}(h | t) - E_{F_c}(h | t') = \int [E(h | t, W, X) - E(h | t', W, X)] dF_c(W, X),$$

Applying the results of the experiment to a new population, forecasting the effects of tax rates not previously experienced, requires the same types of adjustments described in Lecture 2.

Decompose  $E(h | t, W, X)$  into  $h(\cdot)$  and  $G(\cdot)$

Additive Separability Helps

$$h = h(W, t, X) + \varepsilon,$$

$$E(h | W, X, t) - E(h | W, X, t') = h(W, X, t) - h(W, X, t').$$

Treatment effect is the difference between two Marshallian causal functions.

Specialize the Marshallian causal functions

$$h = \alpha_0 + \alpha_1 \ln(W(1-t)) + \alpha_2' X + \varepsilon = \alpha_0 + \alpha_1 \ln W + \alpha_1 \ln(1-t) + \alpha_2' X + \varepsilon.$$

$$E(h | W, t, X) - E(h | W, t', X) = \alpha_1 [\ln(1-t) - \ln(1-t')]$$

$\alpha_1$  is identifiable from the treatment effects.

Randomization governed by (A-5) does not identify  $\alpha_2$ . Generally,  $\varepsilon$  and  $W$  are stochastically dependent, variation induced in  $T$  a randomization that implements (A-5) does not make  $W$  or  $X$  exogenous.

**Social experiments only identify treatment terms and terms that interact with treatment.**

Main effects for  $(W, X)$  not identified. Thus consider the additively separable case  $h(W, X, t, \varepsilon) = h(W, X, t) + \varepsilon$ .

Under it we can recover  $h(W, X, t) - h(W, X, t')$ .

Decompose  $h(W, X, t)$  into a main effect  $\varphi(W, X)$ ,

an interaction term plus main effect for treatment term  $\eta(W, X, t)$

May write  $h(W, X, t) = \varphi(W, X) + \eta(W, X, t)$ .

$\varphi(W, X)$  differences out all contrasts.

Only differences in  $\eta(W, X, t)$  can be identified.

Randomization identifies the treatment effect (not by creating exogeneity between “right hand” variables and error term and identifying Marshallian causal parameters) by **balancing the bias**.

A consequence of (A-5)

$$E(\varepsilon | t', W, A) = E(\varepsilon | t, W, A).$$

“Control functions” (or conditional bias terms) balance of the bias.

If we seek to project the findings from one experiment to a new population with the same, task is greatly simplified by assuming

$$\varepsilon \perp\!\!\!\perp (W, X).$$

No longer necessary to determine distribution of  $\varepsilon$  given  $W, X$  ( $G(\varepsilon | W, X)$ )

## 1.4 Identifying Assumptions For Three Commonly Implemented Types of Social Experiments

Consider three commonly implemented forms of social experiments motivated by the goal of evaluating entire programs or “treatments.” Three populations or subpopulations on which randomization is suggested are:

- (a) the entire population;
- (b) a choice based population of persons who would participate in the program being evaluated in the absence of randomization and
- (c) a population of persons eligible for the program.



Two key identifying assumptions for all methods are:

- (1) that assignment to treatment, or eligibility status conditional on observables does not depend on unmeasured variables that affect outcomes
- (2) the outcomes studied and the populations participating in the program being evaluated are not affected by randomization.

**Assume  $J + 1$  Choices.**

$A_j(\omega) = 1$  if person in a designated population is randomized into program  $j$ .

$A_0(\omega) = 1$  if person is not assigned to any treatment.

$T_j(\omega)$  denotes actual receipt of treatment  $j$ .

Counterfactual treatment participation indicators in world without randomization, denoted  $D_j(\omega)$ .

Full compliance:

$$A_j(\omega) = T_j(\omega). \tag{A-1}$$

Assignment to  $j$  implies treatment  $j$  is received.

Persons assigned treatment  $j$  ( $A_j(\omega) = 1$ ) complying with assignment  $j$  ( $T_j(\omega) = 1$ ) have chosen treatment  $j$  in the counterfactual world ( $D_j(\omega) = 0$ ).

Assumption about assignment by randomization:

$$Pr(A_j(\omega) = 1 \mid X(\omega), \varepsilon(\omega)) = Pr(A_j(\omega) = 1 \mid X(\omega)).$$

Conditional on  $X(\omega)$  assignment to treatment does not depend on  $\varepsilon(\omega)$ .

Alternatively,

$$\Pr(A_j(\omega) = 1 \mid X(\omega), \{Y_i(\omega)\}_{i=0}^J) = \Pr(A_j(\omega) = 1 \mid X(\omega)).$$

Full compliance assumption (A-1): can replace  $A_j(\omega)$  by  $T_j(\omega)$ .

(A-2) ensures that assignment to treatment is not made on the basis of unobservables.

The mechanism used to enforce (A-2) need not be randomization.

Randomization produces information about the program of interest operating under usual conditions provided that it does not alter behavior. This idea is formalized in a third assumption.

Let  $A = (A_0(\omega), \dots, A_J(\omega))$  and  $Y = (Y_0(\omega), \dots, Y_J(\omega))$ .

**Absence of randomization bias:**

(A-3)  $Y$  invariant to mechanism of assignment or selection of outcome.

(Recall Handbook discussion.)



## 1.5 Randomization On Choice Based Subpopulations

Full compliance assumption (A-1) is very strong.

In a social setting, it is difficult to force people to participate in a program to secure compliance.

Randomization is often attempted on subpopulations of persons for whom  $D_j(\omega) = 1$  *i.e* persons who would have gone into program  $j$  in the absence of randomization.

This form of randomization is usually operationalized by administering it to people who apply, and are accepted into a program.

Process of randomization may alter the composition of the population that would apply and be accepted into the program.

Parallel set of potential treatment and outcome variables  $\{D_j^R\}_{j=0}^J$  and  $\{Y_j^R\}_{j=0}^J$ , indexed by  $R$

Let  $T_j(\omega)$  denote actual treatment choice in the presence of randomization.

## Full compliance requires

$$A_j(\omega) = T_j(\omega), j = 0, \dots, J$$

$$A_j(\omega) = T_j(\omega) = 0, T_0(\omega) = 1, j = 0, \dots, J.$$

This method of randomization assumes that persons randomized out of treatment  $j$  forces persons into the no treatment state.

Method assumes that assignment is made on the basis of observables:

$$\begin{aligned}\Pr(A_j(\omega) = 1 \mid X(\omega), \{Y_j^R(\omega)\}_{j=0}^J, D_j^R = d_j^R) \\ = \Pr(A_j(\omega) = 1 \mid X(\omega), D_j^R = d_j^R)\end{aligned}$$

Observe (through application and acceptance) persons who apply to  $j$  in a regime of randomization.

Population generated by this randomization rule.

Random sample of  $(Y_j^R, Y_0^R)$  for  $D_j^R = 1$ .

To ensure that randomization generates the participants and outcomes associated with the usual no-randomization regime,

$$(A-2a) \quad D_j^R(\omega) = D_j(\omega) \quad j = 0, \dots, J$$

$$Y_\ell^R(\omega) = Y_\ell(\omega) \parallel D_j(\omega) = 1, \quad j = 0, \dots, J, \ell = 0, \dots, L.$$

Distribution of observed characteristics is the same in both the usual regime (with the “ $R$ ” superscript) and in the randomized regime:

$$F(x \mid D_j^R = 1) = F(x \mid D_j = 1), \quad j = 0, \dots, J.$$

Can weaken these assumptions if we assume homogeneity in response to treatment “common coefficient model”:

$$Y_j(\omega) - Y_0(\omega) = \Delta_{j,0},$$

Effect of the treatment is the same as everyone.

(Invariance through homogeneity)

## 1.6 Randomization of Eligibility

Randomization of eligibility creates samples that can be used to infer choice probabilities among competing programs.

Let  $e_j = 1$  denote eligibility for participation in treatment  $j$ .

First assume that denial of eligibility for  $j$  implies that a person is embargoed from taking any other treatment.

Later we consider the case where a person is free to select treatments other than  $j$ .

Assume full compliance so that

$$(A-4) \quad e_j(\omega) = 0 \implies T_j(\omega) = 0 \text{ and } T_0(\omega) = 1.$$



Assumption that justifies this type of randomization

$$(A-5) \Pr(e_j = 1 \mid X, \{Y_\ell\}_{\ell=0}^J) = \Pr(e_j = 1 \mid X), \quad j = 1, \dots, J,$$

If eligibility is determined for only for one treatment, say  $j$ , and the purpose is to compare outcomes we can get by with a weaker requirement:

$$\Pr(e_j = 1 \mid X, (Y_0, Y_j)) = \Pr(e_j \mid X), \quad j = 1, \dots, J.^4$$

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<sup>4</sup>The condition would be modified to  $\Pr(e_j = 1 \mid X, Y_\ell, Y_j) = \Pr(e_j = 1 \mid X)$  for studying treatment  $\ell, j$  comparisons.

Changing the population of eligible persons can in principle change the program being studied compared to how it would operate without such eligibility restrictions.

*Sufficient* conditions ensure that randomization of eligibility does not disrupt the normal operations of the program.

“*e*” as a superscript denote random variables

Sufficient set of conditions for randomization of eligibility to be non-disruptive is that

$$(A-6) \quad D_j^e(\omega) = D_j(\omega) \quad j = 0, \dots, J$$

$$Y_j^e(\omega) = Y_j(\omega) \quad j = 0, \dots, J$$

$F(x \mid D_j^e = 1) = F(x \mid D_j = 1)$  distribution of the  $X$  is the same for potential participants

Under (A-6), persons self-select (or are selected) into program in the usual way.

Randomization of eligibility creates a population of persons for whom  $e_j(\omega) = 0$ ,  $T_j(\omega) = 0$  and  $T_0(\omega) = 1$

Population consists of two groups of persons:

those who would have taken treatment  $j$  ( $D_j(\omega) = 1$ ),

those who would not ( $D_j(\omega) = 0$ ) in the absence of randomization of eligibility.

For those made ineligible, we obtain  $Y_0(\omega)$ .

Can identify

$$F(y_0 | X = x) = F(y_0 | X = x, e_j = 0)$$

for all persons irrespective for their  $D_j$  value. By Law of iterated expectations, decompose this into  $J + 1$  components:

$$(3-17) \quad F(y_0 | X = x) = \sum_{\ell=0}^J F(y_0 | D_\ell = 1, X = x) \Pr(D_\ell = 1 | X = x).$$

For those made eligible, we obtain

$$(3-18) \quad F(y(j) \mid D_j^e = 1, X = x, e_j = 1) \\ = F(y(j) \mid D_j = 1, X = x), \quad j = 1, \dots, J$$

$$(3-19) \quad F(y_0 \mid D_j^e = 0, X = x, e_j = 1) = F(y_0 \mid D_j = 0, X = x).$$

From the eligible sample, determine the choice probabilities

$$(3-20) \quad \Pr(D_j = 1 \mid X, e_j = 1) = \Pr(D_j = 1 \mid X).$$

For the case of one treatment,  $J = 1$ , we obtain from the ineligible sample

$$F(y_0 \mid D_0 = 1, X = x) \Pr(D_0 = 1 \mid X = x) \\ + F(y_0 \mid D_1 = 1, X = x) \Pr(D_1 = 1 \mid X = x).$$

Supplement the data from the experiment with the additional information from nonexperimental data,

$(F(y_0 \mid D_0 = 1, X = x), \text{ identify } F(y_0 \mid D_1 = 1, X = x)).$

For the case  $J > 1$ , acquire only the combination of potential outcome distributions.

Even supplementing this with the information from nonexperimental data  $F(y_0 | D_0 = 1, X)$ , we obtain less information on outcome distributions than is obtained under randomization scheme two.

The information can be used to bound distributions but not to exactly identify them.

In this sense, randomization of eligibility for the case  $J > 1$  is less informative than randomization at the stage of application and acceptance, case two experimentation.



Another type of randomization of eligibility denies access to program  $j$  but permits participation in all other programs. Enables analysts to estimate  $\Pr(D_\ell = 1 \mid X)$  facilitates identification of the choice probabilities over what can be obtained in the nonexperimental case by varying the choice sets of participants randomized out of eligibility (see *e.g.* Falmage, 1990).

Assuming full compliance this form of randomization recovers

$$F(y_\ell \mid D_\ell^{e_j=0} = 1, X = x, e_j = 0) = F(y_\ell \mid D_\ell^{e_j=0} = 1, X = x)$$

$$\ell = 0, \dots, J, \quad \ell \neq j, j = 1, \dots, J.$$

$D_\ell^{e_j=0}$  is choice made when choice  $j$  is removed from the choice set. For persons denied eligibility from  $j$ , where  $D_\ell^{e_j=0}$  is informative about outcomes of participants in a counterfactual world when choice  $j$  is eliminated and people are free to select among competing alternatives, including no alternative at all.

Compared with ordinary observational data, obtain information about such objects as

$$E(Y_\ell | D_\ell^{e_j=0} = 1, X = x) - E(Y_\ell | D_\ell = 1, X = x)$$

This experimental not informative about a variety of useful counterfactual distributions:

$$F(y_m | D_\ell = 1, X = x), m \neq \ell, m, \ell \neq j$$

## 1.7 The Data Generated By The Three Kinds of Social Experiment In Comparison With What Is Produced From Nonexperimental Data

Without additional information imposed, there is no information on joint distributions of outcomes.

For the case  $J = 1$ , we observe  $F(y_0 | X), F(y_1, X)$  from Type I random assignment, do not identify  $F(y_0, y_1 | X)$ .

Conventional way to obtain joint distributions is to assume a “unit additivity” model:

$$Y_\ell(\omega) - Y_j(\omega) = \Delta_{\ell j}, \quad \ell \neq j, \ell, j = 0, \dots, J$$

where the  $\Delta_{\ell j}$  are constants. Alternatively, it can be a constant conditional on  $X = x$ .

Type I and Type II randomizations do not produce samples that identify choice probabilities.

Case of multiple treatments ( $J > 1$ ), randomization of eligibility does not identify the conditional distributions identified under Type II randomization.

Augmenting this information with non-experimental data, identifies

$$\sum_{\ell=1}^J F(Y_{\ell} \mid D_{\ell} = 1, X = x) \Pr(D_{\ell} = 1 \mid X = x).$$

Each of the three types of experimental data can be supplemented with non-experimental data law of iterated expectations

$$F(Y_0 | X) = F(Y_0 | D_0 = 1, X = x) \Pr(D_0 = 1 | X = x) \\ + F(Y_0 | D_1 = 1, X = x) \Pr(D_1 = 1 | X = x).$$

From the nonexperimental data, we can identify the probabilities and

$F(Y_0 | D_0 = 1, X = x)$ . Thus we can identify

$$\begin{aligned} & F(Y_0 | D_1 = 1, X = x) \\ &= \frac{F(Y_0 | X = x) - F(Y_0 | D_0 = 1, X = x) \Pr(D_0 = 1 | X = x)}{\Pr(D_1 = 1 | X = x)} \end{aligned}$$

assuming that  $\Pr(D_1 = 1 | X = x) \neq 0$ .



Thus supplementing the data from a Type I experiment with nonexperimental obtain all of the information available from a Type II randomization. By similar reasoning, using nonexperimental data we can obtain more information than is obtained from a Type II randomization:

$$F(Y_1 \mid D_0 = 1, X = x),$$

is obtained, because

$$\begin{aligned} F(Y_1 \mid X = x) &= F(Y_1 \mid D_1 = 1, X = x) \Pr(D_1 = 1 \mid X = x) \\ &\quad + F(Y_1 \mid D_0 = 1, X = x) \Pr(D_0 = 1 \mid X = x). \end{aligned}$$

This analysis does not generalize to the case  $J > 1$ .

$$(3-21) \quad F(Y_\ell | X = x) = \sum_{\ell=0}^J F(y_\ell | D_j = 1, X = x)$$
$$\Pr(D_j = 1 | X = x), \quad \ell = 0, \dots, J, j = 0, \dots, J .$$

Nonexperimental data, we observe

$$F(Y_j | D_j = 1, X = x) \quad j = 0, \dots, J$$

## 1.8 Marginal Experimentation

Frequently of interest to evaluate the effects of variation in policy variables  $Z$  within a program (Electricity Experiments)

Let  $Y$  be an outcome of interest and define a Marshallian causal function

$$Y(\omega) = g(X(\omega)).$$

$X(\omega)$  into  $X_0(\omega)$  and  $X_u(\omega)$ ,  $X_0(\omega)$  of  $X_u(\omega)$  :

$$X_0(\omega) \perp\!\!\!\perp X_u(\omega).$$

excluded variables  $Z(\omega)$

$$Z(\omega) \perp\!\!\!\perp X_u(\omega).$$

In place of randomization, we may assign  $X_0(\omega)$

$$(3-22) \quad X_0(\omega) = H(Z(\omega))$$

additively separable

$$g : g(X(\omega)) = g_0(X_0(\omega)) + g_u(X_u(\omega))$$

$$E(Y(\omega) \mid X_0(\omega) = x_0) = \int g(x_0, X_u(\omega)) dF_u(X_u(\omega))$$

## **1.9 Non-compliance, Attrition and Selection Bias**

### **1.10 Randomization Bias and Substitution Bias**

**Table 1**  
**Information Obtained From Different Experiments and From**  
**Nonexperimental Data Under Full Compliance and Other**  
**Identification Conditions**

|  | Type I<br>Random Assignment<br>To the General<br>Population | Type II<br>Random Assignment<br>Among Accepted<br>Applicants                | Type III<br>Random Assignment<br>of Eligibility  | Non-Experimental<br>Data   |
|--|---|---|--|--|
| <b>One Treatment</b><br>$J = 1$              | $F(Y_0   X), F(Y_1   X)$                                    | $F(Y_0   D_1, X = x)$<br>$F(Y_1   D_1, X = x)$                              | $F(Y_0   D_0 = 1)$<br>$F(Y_0   D_1 = 1)$<br>$F(Y_1   D_1 = 1)$<br>$\Pr(D_1 = 1   X)$                   | $F(Y_0   D_1, X = x)$<br>$F(Y_1   D_1, X = x)$<br>$\Pr(D_1 = 1   X = x)$ |
| <b>Mean Treatment<br/>Effect Identified</b>  | $E(Y_1 - Y_0   X)$  | $E(Y_1 - Y_0   D_1 = 1, X)$   | $E(Y_1 - Y_0   D = 1, X)$  | None in general  |
| <b>Multiple<br/>Treatments</b><br>$J > 1$    | $F(Y_l   X),$<br>$l = 0, \dots, J$                          | $F(Y_0   D_l = 1, X = x)$<br>$F(Y_l   D_l = 1, X = x)$<br>$l = 0, \dots, J$ | $F(Y_l   D_l = 1, X)$<br>$\sum_{l=0}^L F(Y_0   D_l = 1, X)$<br>$\Pr(D_l = 1   X)$<br>$l = 0, \dots, L$ | $F(Y_l   D_l = 1, X = x)$<br>$\Pr(D_l = 1   X = x)$<br>$l = 0, \dots, J$ |
| <b>Mean Treatment<br/>Effects Identified</b> | $E(Y_l   X) - E(Y_j   X)$<br>$l, j = 0, \dots, J$           | $E(Y_l - Y_0   D_l = 1, X)$<br>$l = 0, \dots, J$                            |  | None in general  |

# Experiments

(a) Disrupt Environments

(Heckman, 1992; Hotz, 1992)

Randomization Bias

(b) Do not capture entry effects

(Heckman 1992; Moffit 1992)

(c) Substitution Bias

(Heckman, Hohmann and Khoo)

TABLE 3  
 Treatment Group Dropout and Control Group Substitution  
 in Experimental Evaluations of Active Labor Market Policies  
 [Fraction of Experimental Treatment and Control Groups Receiving Services]

| <u>Study</u>            | <u>Authors/Time Period</u>  | <u>Target Group(s)</u>                       | <u>Fraction of Treatments Receiving Services</u> | <u>Fraction of Controls Receiving Services</u> |
|-------------------------|---|--|--|--|
| 1. NSW*                 | <u>Hollister, et al. (1984)</u><br><u>(9 months after RA)</u>               | <u>Long Term AFDC Women</u>                  | <u>0.95~</u>                                     | <u>0.11</u>                                    |
|                         |   | <u>Ex-addicts</u>                            | <u>NA</u>  | <u>0.03</u>                                    |
|                         |   | <u>17 - 20 year old H.S. dropouts</u>        | <u>NA</u>  | <u>0.04</u>                                    |
| 2. SWIM                 | <u>Friedlander and Hamilton (1993)</u><br><u>(Time period not reported)</u> | <u>AFDC Women: Applicants and Recipients</u> |  |  |
|                         |   | <u>a. Job Search Assistance</u>              | <u>0.54</u>                                      | <u>0.01</u>                                    |
|                         |   | <u>b. Work Experience</u>                    | <u>0.21</u>                                      | <u>0.01</u>                                    |
|                         |   | <u>c. Classroom Training/OJT</u>             | <u>0.39</u>                                      | <u>0.21</u>                                    |
|                         |   | <u>d. Any activity</u>                       | <u>0.69</u>                                      | <u>0.30</u>                                    |
|                         |   | <u>AFDC-U Unemployed Fathers</u>             |  |  |
|                         |   | <u>a. Job Search Assistance</u>              | <u>0.60</u>                                      | <u>0.01</u>                                    |
|                         |   | <u>b. Work Experience</u>                    | <u>0.21</u>                                      | <u>0.01</u>                                    |
| 3. JOBSTART             | <u>Cave, et al. (1993)</u><br><u>(12 months after RA)</u>                   | <u>Youth High School Dropouts</u>            |  |  |
|                         |   | <u>Classroom Training/OJT</u>                | <u>0.90</u>                                      | <u>0.26</u>                                    |
| 4. Project Independence | <u>Kemple, et al. (1995)</u><br><u>(24 months after RA)</u>                 | <u>AFDC Women: Applicants and Recipients</u> |  |  |



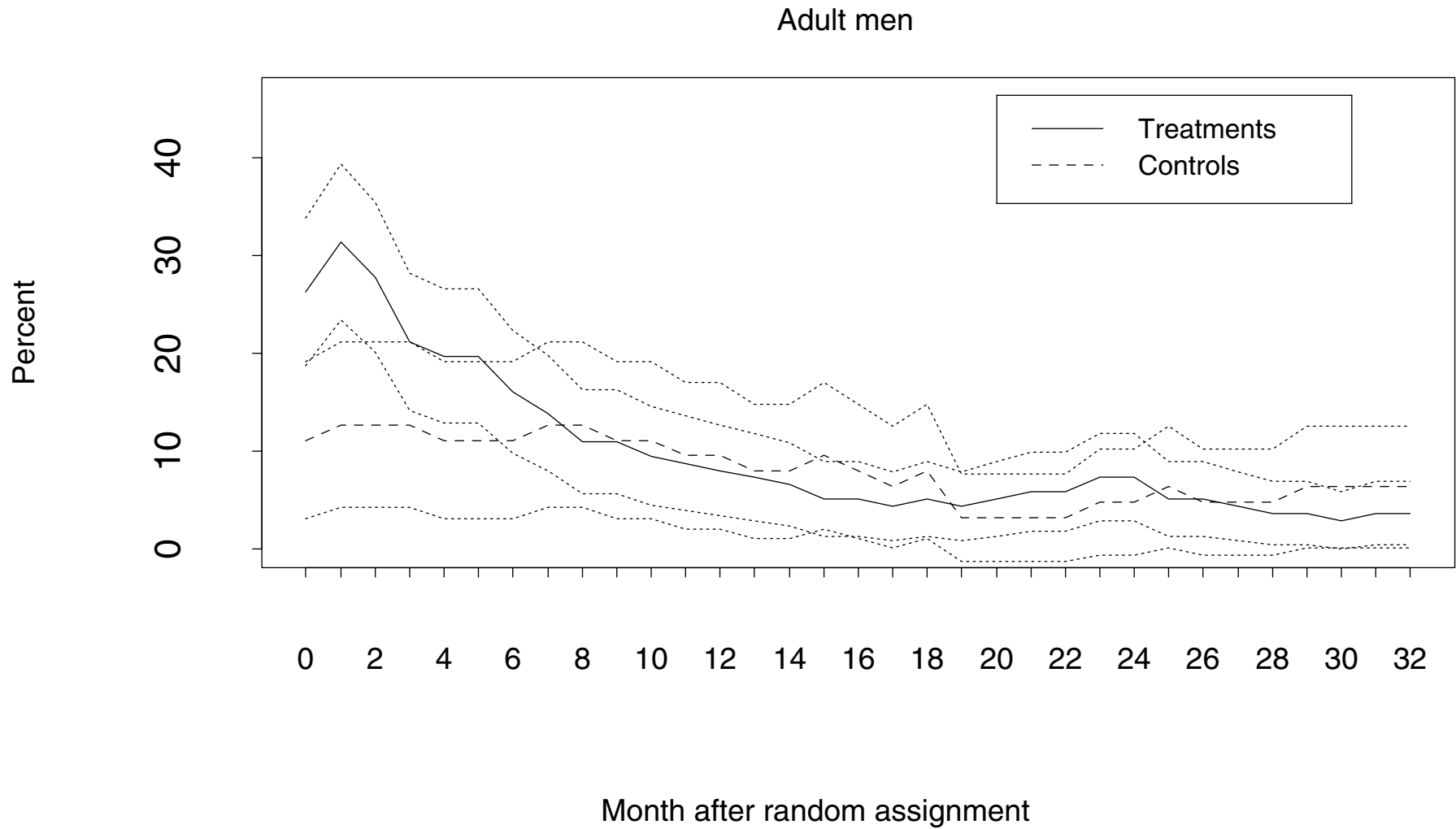
|                      |   |  |             |             |
|----------------------|---|--|-------------|-------------|
|                      |   | <u>a. Job Search Assistance</u>                | <u>0.43</u> | <u>0.19</u> |
|                      |   | <u>b. Classroom Training/OJT</u>               | <u>0.42</u> | <u>0.31</u> |
|                      |   | <u>c. Any activity</u>                         | <u>0.64</u> | <u>0.40</u> |
| <u>5. New Chance</u> | <u>Quint, et al. (1994)</u><br><u>(18 months after RA)</u>                | <u>Teenage Single Mothers</u>                  |             |             |
|                      |   | <u>Any education services</u>                  | <u>0.82</u> | <u>0.48</u> |
|                      |   | <u>Any training services</u>                   | <u>0.26</u> | <u>0.15</u> |
|                      |   | <u>Any education or training</u>               | <u>0.87</u> | <u>0.55</u> |
| <u>6. NJS</u>        | <u>Heckman and</u><br><u>Smith (1998c)</u><br><u>(18 months after RA)</u> | <u>Self-reported from Survey Data</u>          |             |             |
|                      |   | <u>Adult Males</u>                             | <u>0.38</u> | <u>0.24</u> |
|                      |   | <u>Adult females</u>                           | <u>0.51</u> | <u>0.33</u> |
|                      |   | <u>Male youth</u>                              | <u>0.50</u> | <u>0.32</u> |
|                      |   | <u>Female youth</u>                            | <u>0.58</u> | <u>0.41</u> |
|                      |   | <u>Combined Administrative and Survey Data</u> |             |             |
|                      |   | <u>Adult males</u>                             | <u>0.74</u> | <u>0.25</u> |
|                      |   | <u>Adult females</u>                           | <u>0.78</u> | <u>0.34</u> |
|                      |   | <u>Male youth</u>                              | <u>0.81</u> | <u>0.34</u> |
|                      |   | <u>Female youth</u>                            | <u>0.81</u> | <u>0.42</u> |

Notes: RA = random assignment. H.S. = high school. Service receipt includes any employment and training services. The services received by the controls in the NSW study are CETA and WIN jobs. For the Long Term AFDC Women, this measure also includes regular public sector employment during the period.

Sources: Masters and Maynard (1981), p. 148, Table A.15; Maynard (1980), p. 169, Table A14. Friedlander and Hamilton (1993), p. 22, Table 3.1; Cave, et al. (1993), p. 95, Table 4-1; Kemple, et al. (1995), p. 58, Table 3.5; Quint, et al. (1994), p. 110, Table 4.9; Heckman and Smith (1998c) and calculations by the authors.

# Figure 9

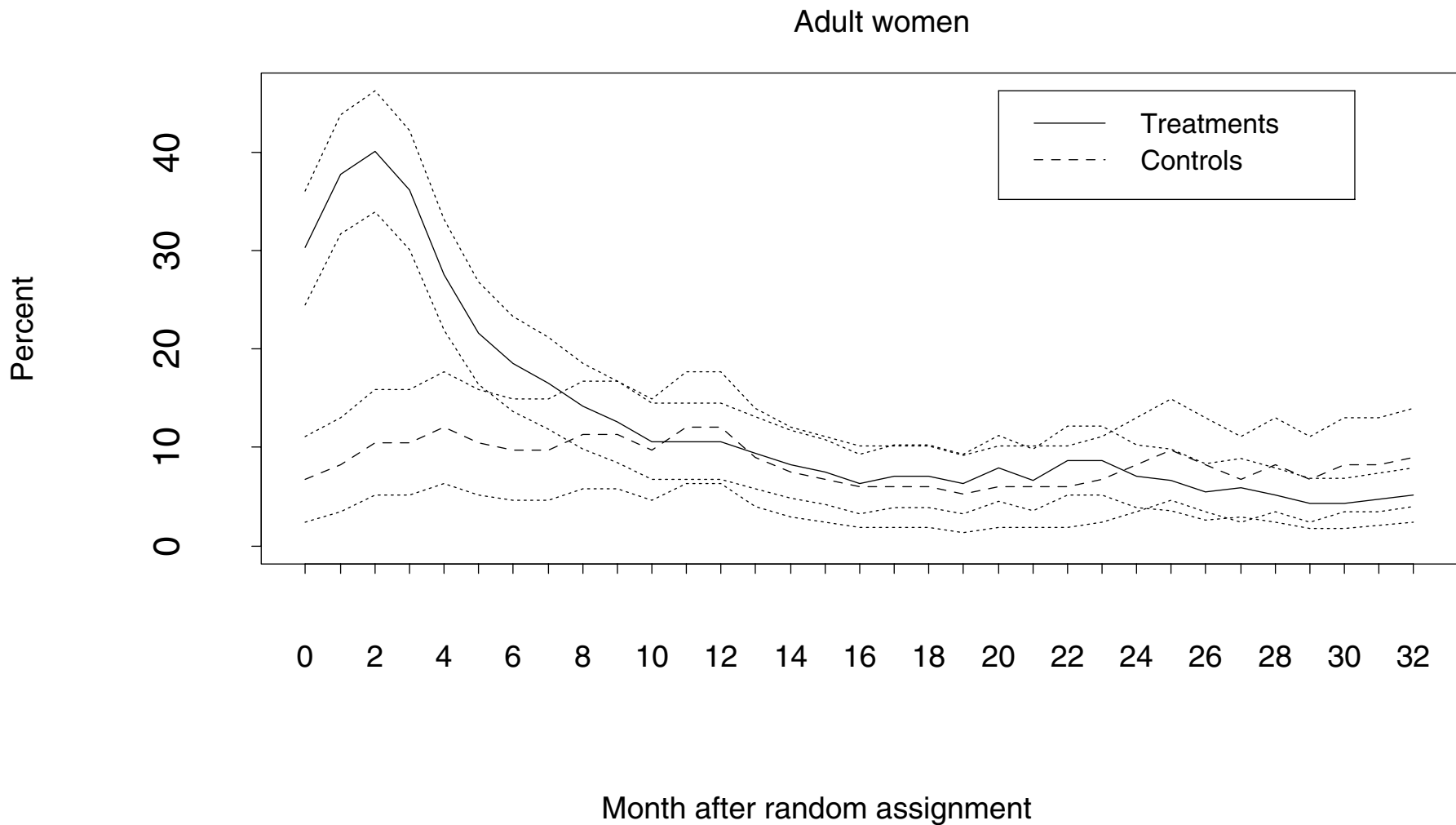
## Percentage Receiving Classroom Training



The percentages are the proportion of persons among the sample who report the receipt of classroom training in each month following random assignment. The sample includes only those persons who responded for the entire 32 months of the survey. Month 0 is the month of random assignment. Standard error bars indicate  $\pm 2$  standard errors about the mean. 66

# Figure 10

## Percentage Receiving Classroom Training



The percentages are the proportion of persons among the sample who report the receipt of classroom training in each month following random assignment. The sample includes only those persons who responded for the entire 32 months of the survey. Month 0 is the month of random assignment. Standard error bars indicate +/- 2 standard errors about the mean.

TABLE I

FRACTION OF EXPERIMENTAL TREATMENT AND CONTROL GROUPS RECEIVING SERVICES  
IN EXPERIMENTAL EVALUATIONS OF EMPLOYMENT AND TRAINING PROGRAMS

| Study                   | Authors/time period   | Target group(s)                       | Fraction of treatments receiving services | Fraction of controls receiving services |
|-------------------------|---|---------------------------------------|---|---|
| 1. NSW                  | Hollister et al. {1984}<br>(9 months after RA)                | Long-term AFDC women                  | 0.95                                      | 0.11                                    |
|                         |   | Ex-addicts                            | NA  | 0.03                                    |
|                         |   | 17–20 year old high school dropouts   | NA  | 0.04                                    |
| 2. SWIM                 | Friedlander and Hamilton (1993)<br>(Time period not reported) | AFDC women: applicants and recipients |   |   |
|                         |   | a. Job search assistance              | 0.54                                      | 0.01                                    |
|                         |   | b. Work experience                    | 0.21                                      | 0.01                                    |
|                         |   | c. Classroom training/OJT             | 0.39                                      | 0.21                                    |
|                         |   | d. Any activity                       | 0.69                                      | 0.30                                    |
|                         |   | AFDC-U Unemployed fathers             |   |   |
|                         |   | a. Job search assistance              | 0.60                                      | 0.01                                    |
|                         |   | b. Work experience                    | 0.21                                      | 0.01                                    |
| 3. JOBSTART             | Cave et al. {1993}<br>(12 months after RA)                    | Youth high school dropouts            |   |   |
|                         |   | Classroom training/OJT                | 0.90                                      | 0.26                                    |
| 4. Project independence | Kemple et al. {1995}<br>(24 months after RA)                  | AFDC women: applicants and recipients |   |   |
|                         |   | a. Job search assistance              | 0.43                                      | 0.19                                    |
|                         |   | b. Classroom training/OJT             | 0.42                                      | 0.31                                    |
| 5. New chance           | Quint et al. {1994}<br>(18 months after RA)                   | c. Any activity                       | 0.64                                      | 0.40                                    |
|                         |   | Teenage single mothers                |   |   |
|                         |   | Any education services                | 0.82                                      | 0.48                                    |
|                         |   | Any training services                 | 0.26                                      | 0.15                                    |
|                         |   | Any education or training             | 0.87                                      | 0.55                                    |

Service receipt includes any employment and training services. RA denotes random assignment to treatment or control groups. In the NSW study, services received by controls are CETA and WIN jobs, for in the Long-term AFDC women group services received also include regular public sector employment. *Sources:* Masters and Maynard (1981), p. 148, Table A.15; Maynard (1980), p. 169, Table A14; Friedlander and Hamilton (1993), p. 22, Table 3.1; Cave et al. (1993), p. 95, Table 4.1; Kemple et al. (1995), p. 58, Table 3.5; Quint et al. (1994), p. 110, Table 4.9.

TABLE II  
CHARACTERISTICS OF CLASSROOM TRAINING IN THE 19 MONTHS FOLLOWING RANDOM ASSIGNMENT

|                                      | Adult men   |         | Adult women        |           | Male youth |                    | Female youth |         |                    |       |
|--------------------------------------|---|---------|--------------------|-----------|------------|--------------------|--------------|---------|--------------------|-------|
|                                      | Treatment   | Control | Prob ( $t >  T $ ) | Treatment | Control    | Prob ( $t >  T $ ) | Treatment    | Control | Prob ( $t >  T $ ) |       |
| Sample size                          | 744   | 325     |                    | 1,697     | 816        |                    | 377          | 174     | 734                | 352   |
| Number receiving CT                  | 363   | 89      |                    | 952       | 272        |                    | 210          | 60      | 430                | 141   |
| Percent receiving CT                 | 48.8%   | 27.4%   | 0.00               | 56.1%     | 33.3%      | 0.00               | 55.7%        | 34.5%   | 58.6%              | 40.1% |
|                                      | Characteristics of persons with one or more training spells |         |                    |           |            |                    |              |         |                    |       |
| Average total months of training     | 6.7   | 7.6     | 0.19               | 7.2       | 8.0        | 0.04               | 7.0          | 6.4     | 6.7                | 7.0   |
| Average total hours of training      | 680.7   | 699.0   | 0.83               | 705.9     | 779.3      | 0.17               | 745.7        | 661.4   | 765.3              | 585.2 |
| Average hours per month of training  | 110.3   | 93.5    | 0.04               | 100.5     | 91.4       | 0.01               | 110.2        | 109.5   | 108.8              | 87.3  |
| Fraction of training months employed | 50.2%   | 46.9%   | 0.77               | 34.7%     | 38.1%      | 0.51               | 47.8%        | 59.2%   | 32.8%              | 48.0% |
| Percent paying for training          | 16.8%   | 41.6%   | 0.00               | 11.6%     | 39.0%      | 0.00               | 16.7%        | 48.3%   | 13.0%              | 36.2% |
| Average monthly payment              | \$209   | \$358   | 0.44               | \$25      | \$101      | 0.00               | \$39         | \$103   | \$43               | \$226 |

The sample is rectangular and includes all persons from the sixteen experimental sites with valid data on training receipt.  $T$ -tests are of the null hypothesis that the means of the treatment and control samples are equal within demographic groups. Classroom training payments are the amount paid by the entire household. Average payments are for each trainee and include trainees who reported zero expenditures.

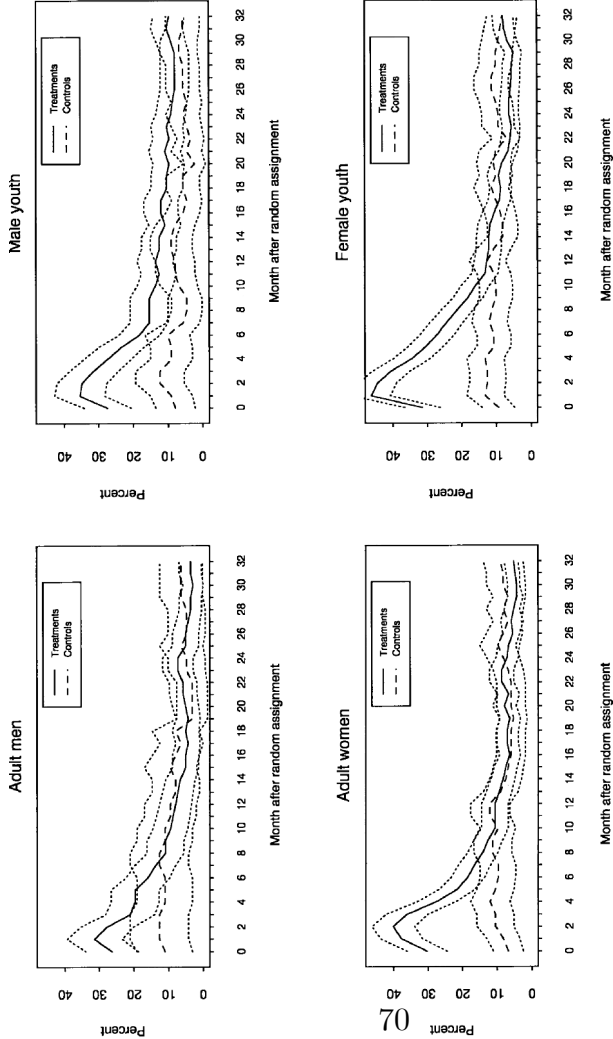


FIGURE I

Percentage Receiving Classroom Training

The percentages are the proportion of persons among the sample who report the receipt of classroom training in each month following random assignment. The sample includes only those persons who responded for the entire 32 months of the survey. Month 0 is the month of random assignment. Standard error bars indicate  $\pm 2$  standard errors about the mean.

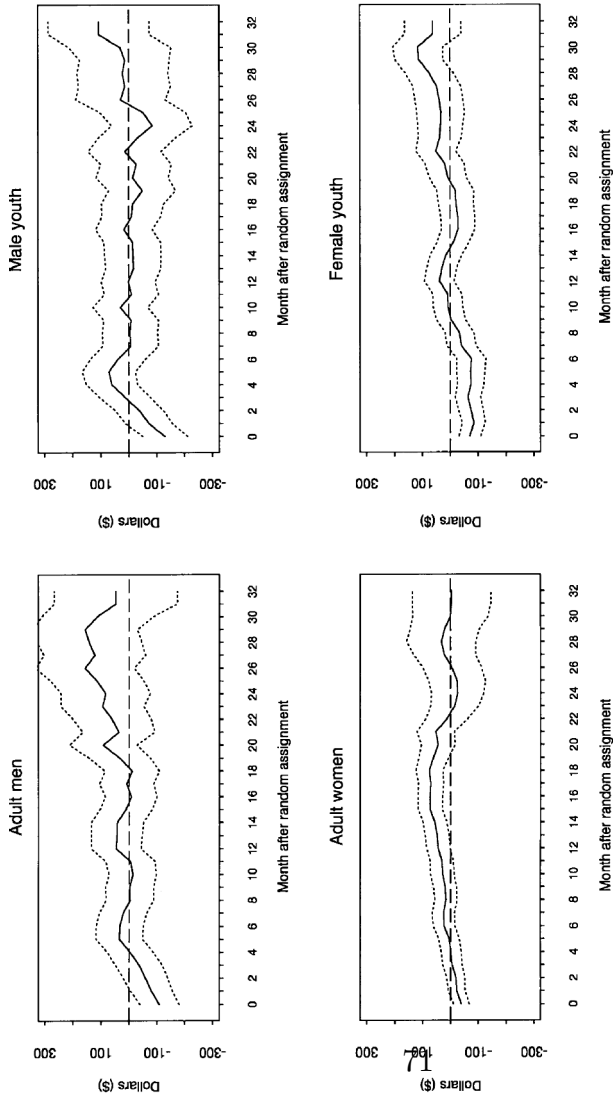


FIGURE II

Experimental Estimates of the Monthly Effect of the JTPA Program

The dependent variable in an OLS regression is self-reported monthly earnings. The sample consists of all person-months in the 32 months after random assignment (RA) with valid values for all variables. Regressors include indicators for treatment status, calendar month, month after RA, treatment status\*month after RA, race, marital status, education, training center of random assignment, age, and English language preference. The top 1 percent of earnings values are dropped in each month in both the treatment and control groups. Standard error bars indicate  $\pm 2$  Eicher-White robust standard errors about the mean.

TABLE III  
 MEAN DISCOUNTED EARNINGS AND ESTIMATES OF THE DISCOUNTED RETURNS TO THE JTPA PROGRAM  $R_0$

| $r$  | Adult males                                |         |          | Adult females |         |          | Youth males |         |          | Youth females |         |          |
|------|--|---------|----------|---------------|---------|----------|-------------|---------|----------|---------------|---------|----------|
|      | 33 months                                  | 5 years | 10 years | 33 months     | 5 years | 10 years | 33 months   | 5 years | 10 years | 33 months     | 5 years | 10 years |
| 0    | 25625                                      | 49303   | 101921   | 12737         | 25437   | 53659    | 20829       | 41765   | 88288    | 11441         | 22128   | 45877    |
| 0.03 | 24513                                      | 45596   | 87652    | 12163         | 23472   | 46029    | 19883       | 38525   | 75709    | 10941         | 20457   | 39439    |
| 0.10 | 22149                                      | 38254   | 63369    | 10945         | 19584   | 33054    | 17875       | 32115   | 54321    | 9878          | 17147   | 28483    |
|      | Estimates of the discounted returns        |         |          |               |         |          |             |         |          |               |         |          |
| 0    | 1337                                       | 3949    | 9755     | 787           | 1002    | 1481     | 209         | 491     | 1117     | 269           | 1704    | 4892     |
|      | (102)                                      | (478)   | (1357)   | (57)          | (300)   | (860)    | (102)       | (409)   | (1146)   | (58)          | (231)   | (642)    |
| 0.03 | 1248                                       | 3574    | 8214     | 755           | 947     | 1330     | 190         | 441     | 942      | 222           | 1500    | 4048     |
|      | (98)                                       | (430)   | (1132)   | (54)          | (270)   | (717)    | (97)        | (369)   | (957)    | (55)          | (209)   | (536)    |
| 0.10 | 1061                                       | 2838    | 5609     | 687           | 833     | 1062     | 152         | 343     | 642      | 125           | 1101    | 2623     |
|      | (87)                                       | (338)   | (756)    | (48)          | (211)   | (478)    | (88)        | (291)   | (640)    | (49)          | (165)   | (360)    |
|      | Estimates of the internal rates of returns |         |          |               |         |          |             |         |          |               |         |          |
|      | 1.17                                       | 1.27    | 1.28     | 2.63          | 2.63    | 2.63     | 0.66        | 0.79    | 0.80     | 0.21          | 0.53    | 0.58     |

Discounted earnings are the present discounted value of mean monthly control group earnings discounted at  $1/(1+r)$ , where  $r$  ranges over 0, 0.03, and 0.10. Estimates of  $R_0$  are the present discounted value of the effect of the program based on program effects with the indicated durations. Monthly earnings beyond the 33-month sample are set at the mean level of months 22 to 33 after random assignment. Estimates are of private returns and include estimated average monthly tuition payments. The internal rate of return is the annual rate of return  $r$  such that the net present value of the earnings/cost stream, discounted at  $1/(1+r)$ , is equal to zero. Rates of return are reported as fractions, *not as percentages*. Internal rate of return estimates are also private estimates and so include the estimated monthly tuition payments. Estimated standard errors appear in parentheses.



TABLE IV  
ESTIMATES OF THE DISCOUNTED RETURNS TO JTPA TRAINING  $R_1$

| $r$  | Adult males  |                 |                 | Adult females |                |                | Youth males  |                |                | Youth females |                 |                 |
|------|--|-----------------|-----------------|---------------|----------------|----------------|--------------|----------------|----------------|---------------|-----------------|-----------------|
|      | 33 months  | 5 years         | 10 years        | 33 months     | 5 years        | 10 years       | 33 months    | 5 years        | 10 years       | 33 months     | 5 years         | 10 years        |
| 0    | 5268<br>(530)  | 17429<br>(2737) | 44454<br>(7873) | 3687<br>(251) | 4622<br>(1221) | 6700<br>(3474) | 847<br>(526) | 2203<br>(2149) | 5218<br>(5980) | 2929<br>(296) | 12186<br>(1511) | 32756<br>(4318) |
| 0.03 | 4862<br>(504)  | 15690<br>(2460) | 37290<br>(6562) | 3538<br>(238) | 4371<br>(1098) | 6032<br>(2898) | 754<br>(500) | 1962<br>(1937) | 4371<br>(4995) | 2608<br>(281) | 10850<br>(1359) | 27292<br>(3601) |
| 0.10 | 4012<br>(450)  | 12284<br>(1925) | 25183<br>(4369) | 3215<br>(211) | 3851<br>(861)  | 4843<br>(1933) | 564<br>(446) | 1487<br>(1526) | 2926<br>(3346) | 1947<br>(248) | 8243<br>(1064)  | 18061<br>(2401) |
|      | Estimates of discounted returns adjusted by training incidence           |                 |                 |               |                |                |              |                |                |               |                 |                 |
| 0    | 3739<br>(427)  | 12367<br>(1676) | 31542<br>(4654) | 3875<br>(274) | 5114<br>(1501) | 7868<br>(4325) | 758<br>(467) | 2071<br>(2013) | 4989<br>(5641) | 1281<br>(200) | 6998<br>(959)   | 19702<br>(2729) |
| 0.03 | 3446<br>(408)  | 11129<br>(1512) | 26454<br>(3889) | 3714<br>(259) | 4818<br>(1348) | 7019<br>(3604) | 670<br>(444) | 1839<br>(1813) | 4172<br>(4710) | 1088<br>(190) | 6178<br>(863)   | 16332<br>(2276) |
| 0.10 | 2831<br>(368)  | 8700<br>(1195)  | 17852<br>(2608) | 3366<br>(228) | 4209<br>(1053) | 5523<br>(2398) | 491<br>(395) | 1385<br>(1426) | 2777<br>(3150) | 690<br>(169)  | 4579<br>(677)   | 10642<br>(1519) |
|      | Estimates of the internal rates of return adjusted by training incidence |                 |                 |               |                |                |              |                |                |               |                 |                 |
|      | 0.79   | 0.96            | 0.97            | 2.45          | 2.45           | 2.45           | 0.45         | 0.62           | 0.65           | 0.43          | 0.70            | 0.73            |
|      | Estimates of the internal rates of return adjusted by training hours     |                 |                 |               |                |                |              |                |                |               |                 |                 |
|      | 0.73   | 0.90            | 0.91            | 2.44          | 2.44           | 2.44           | 0.41         | 0.59           | 0.62           | 0.26          | 0.56            | 0.61            |

Estimates based on incidence of classroom training receipt are constructed using estimated monthly program effects ( $\Delta_s$ ) adjusted upward by  $1/(p_s - q_s)$ , where  $p_s$  is the proportion of treatments who have received some level of classroom training by month  $s$ , and  $q_s$  is defined similarly for controls. Estimates based on hours of classroom training receipt are constructed using estimated monthly program effects ( $\Delta_s$ ) adjusted upward by  $1/(p_s - q_s)$ , where  $p_s$  is the average cumulative hours of classroom training received by treatments by month  $s$ , and  $q_s$  is defined similarly for controls. These constant hourly impact figures are then multiplied by the average cumulative hours of classroom training received by treatments who report at least one CT training spell by month  $s$  (i.e., treatments who actually receive training) to yield the monthly effect of training based on constant hourly effects. Monthly earnings beyond the 33-month sample are set at the mean level of months 22 to 33 after random assignment. Estimates are of private returns and include estimated average monthly tuition payments. The internal rate of return is the annual rate of return  $r$  such that the net present value of the earnings/cost stream, discounted at  $1/(1 + r)$ , is equal to zero. Estimated standard errors appear in parentheses.

TABLE V  
NONEXPERIMENTAL ESTIMATES OF THE MONTHLY EFFECTS OF TRAINING  $\Delta_d$  AND  $\Delta_o$  ON TREATMENT GROUP MEMBERS

|                    | Adult males                   |                   | Adult females  |                   | Youth males                   |                   | Youth females                 |                   |
|--------------------|-------------------------------|-------------------|--|-------------------|-------------------------------|-------------------|-------------------------------|-------------------|
|                    | Difference-<br>in differences | Cross-<br>section | Difference-<br>in differences  | Cross-<br>section | Difference-<br>in differences | Cross-<br>section | Difference-<br>in differences | Cross-<br>section |
| Sample size        | 19438                         |                   | 42943  |                   | 11328                         |                   | 22052                         |                   |
| Mean earnings gain | 777                           |                   | 386  |                   | 632                           |                   | 347                           |                   |
|                    |                               |                   | Estimates of $\Delta_d$ for persons with 1-4 months of training                              |                   |                               |                   |                               |                   |
|                    | -57<br>(75)                   | -231<br>(48)      | -51<br>(32)  | -127<br>(21)      | -17<br>(93)                   | -189<br>(59)      | -57<br>(48)                   | -67<br>(32)       |
|                    |                               |                   | Estimates of $\Delta_d$ for persons with > 4 months of training, having completed 1-4 months |                   |                               |                   |                               |                   |
|                    | -68<br>(59)                   | -273<br>(46)      | -75<br>(25)  | -189<br>(17)      | -129<br>(64)                  | -180<br>(46)      | -66<br>(29)                   | -111<br>(22)      |
|                    |                               |                   | Estimates of $\Delta_d$ for persons with > 4 months of training, having completed > 4 months |                   |                               |                   |                               |                   |
|                    | -96<br>(86)                   | -302<br>(66)      | -117<br>(32)   | -231<br>(24)      | -207<br>(77)                  | -259<br>(62)      | -44<br>(38)                   | -89<br>(29)       |
|                    |                               |                   | Estimates of $\Delta_o$ for persons with 1-4 months of training                              |                   |                               |                   |                               |                   |
|                    | 280<br>(92)                   | 105<br>(55)       | 111<br>(43)  | 36<br>(29)        | 169<br>(107)                  | -3<br>(61)        | 77<br>(57)                    | 66<br>(38)        |
|                    |                               |                   | Estimates of $\Delta_o$ for persons with > 4 months of training                              |                   |                               |                   |                               |                   |
|                    | 230<br>(90)                   | 25<br>(60)        | 215<br>(39)  | 101<br>(31)       | 70<br>(90)                    | 18<br>(55)        | 169<br>(42)                   | 124<br>(33)       |

The dependent variable in the OLS regression is pooled self-reported monthly earnings. The regression sample consists of all person-months for treatments at the sixteen experimental sites in the 33 months after random assignment. (RA) with valid values for all variables. Regressors include indicators for training status, calendar month, month after RA, race, marital status, education, training center of RA, age, and English language preference. The excluded training status is never receiving training. Separate sets of training status indicators are used to estimate effects for training spells of one to four months or more than five months in duration. The top 1 percent of earnings values are dropped in each month. Mean earnings is the mean level of monthly earnings for members of the control group who reported earnings over the full 33-month period. Estimated standard errors appear in parentheses.

TABLE VI

NONEXPERIMENTAL ESTIMATES OF THE DISCOUNTED RETURNS TO TRAINING,  $R_1$  FOR TREATMENT GROUP MEMBERS

| Training length                                  | Adult males |         |          | Adult females |         |          | Youth males |         |          | Youth females |         |          |
|--|-------------|---------|----------|---------------|---------|----------|-------------|---------|----------|---------------|---------|----------|
|  | 33 months   | 5 years | 10 years | 33 months     | 5 years | 10 years | 33 months   | 5 years | 10 years | 33 months     | 5 years | 10 years |
| 3 months   | 7362        | 13349   | 24086    | 2801          | 5175    | 9433     | 4421        | 8044    | 14541    | 1789          | 3428    | 6367     |
|  | (2529)      | (4490)  | (8013)   | (1194)        | (2122)  | (3787)   | (2962)      | (5257)  | (9380)   | (1572)        | (2791)  | (4980)   |
|  | 4964        | 9889    | 18720    | 4601          | 9202    | 17451    | 533         | 2032    | 4719     | 3572          | 7193    | 13685    |
| 6 months   | (2233)      | (4158)  | (7622)   | (972)         | (1811)  | (3321)   | (2216)      | (4126)  | (7562)   | (1046)        | (1949)  | (3572)   |
| Private returns based on before-after estimates  |             |         |          |               |         |          |             |         |          |               |         |          |
| 3 months   | 2730        | 8717    | 19453    | -1884         | 490     | 4749     | -184        | 3440    | 9936     | -2842         | -1203   | 1736     |
|  | (2529)      | (4490)  | (8013)   | (1194)        | (2122)  | (3787)   | (2962)      | (5257)  | (9380)   | (1572)        | (2791)  | (4980)   |
|  | 405         | 5330    | 14161    | -33           | 4568    | 12817    | -3974       | -2476   | 211      | -977          | 2644    | 9136     |
| 6 months   | (2233)      | (4158)  | (7622)   | (972)         | (1811)  | (3321)   | (2216)      | (4126)  | (7562)   | (1046)        | (1949)  | (3572)   |
| Social returns based on before-after estimates   |             |         |          |               |         |          |             |         |          |               |         |          |
| 3 months   | 2066        | 4326    | 8377     | 510           | 1272    | 2639     | -804        | -860    | -959     | 1464          | 2874    | 5403     |
|  | (1503)      | (2668)  | (4761)   | (802)         | (1425)  | (2544)   | (1693)      | (3004)  | (5358)   | (1048)        | (1861)  | (3321)   |
|  | -1277       | -746    | 206      | 1136          | 3298    | 7174     | -1037       | -644    | 62       | 2203          | 4860    | 9624     |
| 6 months   | (1496)      | (2781)  | (5094)   | (766)         | (1429)  | (2620)   | (1361)      | (2526)  | (4625)   | (808)         | (1506)  | (2761)   |
| Private returns based on cross-section estimates |             |         |          |               |         |          |             |         |          |               |         |          |
| 3 months   | -2566       | -307    | 3744     | -4175         | -3413   | -2046    | -5409       | -5464   | -5563    | -3167         | -1757   | 772      |
|  | (1503)      | (2668)  | (4761)   | (802)         | (1425)  | (2544)   | (1693)      | (3004)  | (5358)   | (1048)        | (1861)  | (3321)   |
|  | -5837       | -5306   | -4353    | -3498         | -1336   | 2540     | -5544       | -5151   | -4446    | -2346         | 311     | 5075     |
| 6 months   | (1496)      | (2781)  | (5094)   | (766)         | (1429)  | (2620)   | (1361)      | (2526)  | (4625)   | (808)         | (1506)  | (2761)   |
| Social returns based on cross-section estimates  |             |         |          |               |         |          |             |         |          |               |         |          |
| 3 months   | -2566       | -307    | 3744     | -4175         | -3413   | -2046    | -5409       | -5464   | -5563    | -3167         | -1757   | 772      |
|  | (1503)      | (2668)  | (4761)   | (802)         | (1425)  | (2544)   | (1693)      | (3004)  | (5358)   | (1048)        | (1861)  | (3321)   |
|  | -5837       | -5306   | -4353    | -3498         | -1336   | 2540     | -5544       | -5151   | -4446    | -2346         | 311     | 5075     |
| 6 months   | (1496)      | (2781)  | (5094)   | (766)         | (1429)  | (2620)   | (1361)      | (2526)  | (4625)   | (808)         | (1506)  | (2761)   |

Returns are the present discounted value of the training effect, discounted at  $1/(1+r)$ , where  $r = 0.03$ , and based on estimated monthly effects of training  $\Delta_d$  and  $\Delta_m$ . The duration of training is set at 3 or 6 months and the effects of training persist for either 33 months, 5 years, or 10 years. Private returns include the estimated monthly tuition payments. Social returns include the estimated marginal costs incurred by the training provider, adjusted upward by 1.5 to reflect the deadweight cost of taxation.

TABLE VII  
 NONEXPERIMENTAL ESTIMATES OF THE MONTHLY EFFECTS OF TRAINING  $\Delta_d$  AND  $\Delta_o$  for Control Group Members

| Sample size | Adult males               |   | Adult females             |               | Youth males               |               | Youth females             |               |
|-------------|---------------------------|---|---------------------------|---------------|---------------------------|---------------|---------------------------|---------------|
|             | Difference-in-differences | Cross-section   | Difference-in-differences | Cross-section | Difference-in-differences | Cross-section | Difference-in-differences | Cross-section |
|             | 8696                      | 20815   | 5447                      | 10449         |                           |               |                           |               |
|             |                           | Estimates of $\Delta_d$ for persons with 1-4 months of training                             |                           |               |                           |               |                           |               |
|             | -283<br>(111)             | -107<br>(50)  | -93<br>(75)               | -66<br>(98)   | -138<br>(49)              | -227<br>(44)  |                           |               |
|             |                           | Estimates of $\Delta_d$ for persons with >4 months of training, having completed 1-4 months |                           |               |                           |               |                           |               |
|             | -146<br>(95)              | -86<br>(44)   | -133<br>(101)             | -256<br>(83)  | -9<br>(34)                | -172<br>(38)  |                           |               |
|             |                           | Estimates of $\Delta_d$ for persons with >4 months of training, having completed >4 months  |                           |               |                           |               |                           |               |
|             | -198<br>(120)             | -115<br>(58)  | 10<br>(107)               | -113<br>(93)  | -91<br>(43)               | -254<br>(42)  |                           |               |
|             |                           | Estimates of $\Delta_o$ for persons with 1-4 months of training                             |                           |               |                           |               |                           |               |
|             | 85<br>(141)               | 95<br>(72)  | -3<br>(99)                | 25<br>(70)    | 47<br>(65)                | -42<br>(56)   |                           |               |
|             |                           | Estimates of $\Delta_o$ for persons with >4 months of training                              |                           |               |                           |               |                           |               |
|             | 379<br>(139)              | 116<br>(72)   | 211<br>(115)              | 88<br>(105)   | 238<br>(62)               | 74<br>(58)    |                           |               |

The dependent variable in the OLS regression is pooled self-reported monthly earnings. The regression sample consists of all person-months for controls at the sixteen experimental sites in the 33 months after random assignment with valid values for all variables. Regressors include indicators for training status, calendar month, month after RA, race, marital status, education, training center of random assignment, age, and English language preference. The excluded training status is never receiving training. Separate sets of training status indicators are used to estimate effects for training spells of one to four months or more than five months in duration. The top 1 percent of earnings values are dropped in each month. Estimated standard errors are in parentheses.

TABLE VIII  
NONEXPERIMENTAL ESTIMATES OF THE DISCOUNTED RETURNS TO TRAINING,  $R_1$ , CORRECTED FOR SELECTION

| Adult males  |                 |                  | Adult females  |                 |                 | Youth males     |                 |                   | Youth females   |                 |                  |
|--|-----------------|------------------|----------------|-----------------|-----------------|-----------------|-----------------|-------------------|-----------------|-----------------|------------------|
| 33 months  | 5 years         | 10 years         | 33 months      | 5 years         | 10 years        | 33 months       | 5 years         | 10 years          | 33 months       | 5 years         | 10 years         |
| 1912<br>(387)  | 4226<br>(890)   | 8840<br>(1977)   | 1191<br>(195)  | 3037<br>(456)   | 6719<br>(1016)  | 647<br>(426)    | 1537<br>(991)   | 3313<br>(2205)    | 1843<br>(241)   | 4163<br>(564)   | 8789<br>(1257)   |
| I. Regression-adjusted on X                                  |                 |                  |                |                 |                 |                 |                 |                   |                 |                 |                  |
| 2255<br>(447)  | 4964<br>(1026)  | 10367<br>(2278)  | 2250<br>(234)  | 5085<br>(548)   | 10740<br>(1220) | 1936<br>(573)   | 3897<br>(1342)  | 7809<br>(2991)    | 1186<br>(341)   | 3120<br>(800)   | 6977<br>(1784)   |
| II. Regression-adjusted on X and Z                           |                 |                  |                |                 |                 |                 |                 |                   |                 |                 |                  |
| 1672<br>(516)  | 3901<br>(1111)  | 8348<br>(2436)   | 1527<br>(304)  | 3635<br>(713)   | 7840<br>(1589)  | 1472<br>(926)   | 3081<br>(1856)  | 6291<br>(3999)    | 1917<br>(286)   | 4454<br>(661)   | 9514<br>(1471)   |
| III. Regression-adjusted on X and Z through propensity score |                 |                  |                |                 |                 |                 |                 |                   |                 |                 |                  |
| 8201<br>(2408)   | 14836<br>(5489) | 28071<br>(12171) | 3816<br>(1425) | 9556<br>(3349)  | 21005<br>(7469) | -2407<br>(2071) | -5214<br>(4883) | -10812<br>(10895) | 10520<br>(1944) | 20358<br>(4655) | 39983<br>(10414) |
| IV. Instrumental-variables estimates                         |                 |                  |                |                 |                 |                 |                 |                   |                 |                 |                  |
| 17025<br>(2709)  | 28568<br>(6233) | 51595<br>(13846) | 9343<br>(1582) | 20310<br>(3714) | 42185<br>(8279) | 1074<br>(2118)  | 1331<br>(4985)  | 1845<br>(11119)   | 4466<br>(1637)  | 9346<br>(3828)  | 19079<br>(8528)  |
| V. Heckman (1979) method                                     |                 |                  |                |                 |                 |                 |                 |                   |                 |                 |                  |

Returns are the present discounted value of the estimated monthly effects of training, discounted at  $1/(1+r)$ , where  $r = 0.03$ . The selection-corrected monthly effect of training for treatment group members is estimated through separate regressions for months 0 through 18 after random-assignment (RA). For succeeding months, the effect of training is taken to be the mean of the training effects for months 13-18. In order to isolate the effect of training completion, the sample is restricted to either those who receive no training or those who complete their training within 12 months of RA. The top 1 percent of earnings values in each month are excluded. The dependent variable  $Y$  in each regression is a person's self-reported earnings in that month. Exogenous regressors  $X$  in the earnings equation include indicators for race, marital status, education, size of random assignment, and age.  $T$  is a treatment indicator.  $T = 1$  signifies that an individual has participated in training by the month of the regression. Participation-related regressors  $Z$  include month of random assignment, household size, indicators for progressively higher levels of total family income, and indicators for receipt of adult basic education, vocational training, and job search assistance at or before random assignment. The estimated training effect for Method I is the coefficient on  $T$  in an OLS regression of  $Y$  on  $X$ . For Method II, it is the coefficient on  $T$  in an OLS regression of  $Y$  on  $X$  and  $Z$  (see Heckman, Ichimura, Smith, and Todd (1998)). For Method III, it is the coefficient on  $T$  in an OLS regression of  $Y$  on  $X, P$ , and  $T$ , where  $P$  is the predicted probability of participation from a probit of  $T$  on  $Z$ . (See Heckman and Robb (1986) for discussion of this method.) For Method IV, it is the coefficient on  $T$  in an OLS regression of  $Y$  on  $X$  and  $P$ , where  $P$  is the predicted value from an OLS regression of  $T$  on  $X$  and  $Z$ . For Method V, the Heckman two-step model, it is the coefficient on  $T$  in an OLS regression of  $Y$  on  $X, M$ , and  $T$ , where  $M$  is the estimated inverse Mills ratio from a probit of  $T$  on  $Z$ . The estimated standard error of Method V does not incorporate the additional variance component resulting from the first-stage estimation. Estimated standard errors are in parentheses.

TABLE IX  
ESTIMATED BOUNDS ON THE DISCOUNTED RETURNS TO JTIPA TRAINING  $R_1$

| Adult males  |                  |                   | Adult females   |                 |                   | Youth males     |                  |                   | Youth females   |                 |                   |
|--|------------------|-------------------|-----------------|-----------------|-------------------|-----------------|------------------|-------------------|-----------------|-----------------|-------------------|
| 33 months  | 5 years          | 10 years          | 33 months       | 5 years         | 10 years          | 33 months       | 5 years          | 10 years          | 33 months       | 5 years         | 10 years          |
| -61254<br>(363)  | -113194<br>(688) | -216799<br>(1788) | -48755<br>(179) | -94469<br>(359) | -185655<br>(949)  | -52544<br>(314) | -104590<br>(565) | -208407<br>(1440) | -40457<br>(167) | -79469<br>(300) | -157288<br>(764)  |
| Lower bound with (AS-7) imposed                                  |                  |                   |                 |                 |                   |                 |                  |                   |                 |                 |                   |
| -44294<br>(698)  | -81262<br>(1271) | -155004<br>(3256) | -37048<br>(296) | -73848<br>(572) | -147254<br>(1497) | -41059<br>(578) | -84791<br>(1002) | -172024<br>(2519) | -33611<br>(281) | -68192<br>(470) | -137171<br>(1162) |
| Lower bound with (AS-7) and (AS-8) imposed                       |                  |                   |                 |                 |                   |                 |                  |                   |                 |                 |                   |
| -2214<br>(800)   | -942<br>(1441)   | 1595<br>(3678)    | 1133<br>(373)   | 3002<br>(707)   | 6729<br>(1837)    | -1772<br>(670)  | -2496<br>(1156)  | -3940<br>(2901)   | -1129<br>(341)  | 96<br>(581)     | 2540<br>(1449)    |
| Lower bound with (AS-7), (AS-8), and (AS-9) imposed              |                  |                   |                 |                 |                   |                 |                  |                   |                 |                 |                   |
| 21824<br>(321)   | 40864<br>(628)   | 78842<br>(1648)   | 13007<br>(144)  | 25155<br>(286)  | 49388<br>(753)    | 17160<br>(274)  | 33047<br>(505)   | 64736<br>(1299)   | 11208<br>(141)  | 22186<br>(261)  | 44084<br>(674)    |
| Upper bound with (AS-7) imposed                                  |                  |                   |                 |                 |                   |                 |                  |                   |                 |                 |                   |
| 13015<br>(698)   | 29303<br>(1271)  | 61795<br>(3256)   | 8255<br>(296)   | 15924<br>(572)  | 31222<br>(1497)   | 9609<br>(578)   | 19532<br>(1002)  | 39325<br>(2519)   | 4902<br>(281)   | 11916<br>(470)  | 25909<br>(1162)   |
| Upper bound with (AS-7), (AS-8), and, optionally, (AS-9) imposed |                  |                   |                 |                 |                   |                 |                  |                   |                 |                 |                   |

Estimates of bounds on  $R_1$  are the present discounted value of the estimated monthly bounds on the effect of training less the average monthly cost of training, discounted at  $1/(1+r)$ , where  $r = 0.03$ . Standard errors of  $R_1$  are derived from the discounted sum of individual monthly variance estimates on the training effect bounds. Estimated standard errors are in parentheses.

APPENDIX 1: DEMOGRAPHIC CHARACTERISTICS OF TRAINEES AND NONTRAINEES

|                                       | Adult male trainees    |           |                    | Adult male nontrainees   |           |                    | Adult female trainees |           |                    | Adult female nontrainees |           |                    |
|---------------------------------------|------------------------|-----------|--------------------|--------------------------|-----------|--------------------|-----------------------|-----------|--------------------|--------------------------|-----------|--------------------|
|                                       | Treat-ments            | Con-trols | Prob ( $t >  T $ ) | Treat-ments              | Con-trols | Prob ( $t >  T $ ) | Treat-ments           | Con-trols | Prob ( $t >  T $ ) | Treat-ments              | Con-trols | Prob ( $t >  T $ ) |
| Sample size                           | 363                    | 89        |                    | 381                      | 236       |                    | 952                   | 272       |                    | 745                      | 544       |                    |
| Percent black                         | 33.1%                  | 37.1%     | 0.48               | 42.8%                    | 36.4%     | 0.12               | 27.0%                 | 26.5%     | 0.86               | 40.4%                    | 37.7%     | 0.32               |
| Percent Hispanic                      | 11.0%                  | 10.1%     | 0.80               | 5.0%                     | 11.4%     | 0.01               | 15.9%                 | 17.3%     | 0.58               | 10.1%                    | 11.0%     | 0.58               |
| Percent with 12 years schooling       | 68.6%                  | 77.5%     | 0.08               | 69.8%                    | 67.4%     | 0.53               | 60.5%                 | 63.2%     | 0.41               | 62.6%                    | 59.0%     | 0.20               |
| Percent with > 12 years schooling     | 26.4%                  | 25.8%     | 0.91               | 23.1%                    | 22.5%     | 0.85               | 16.6%                 | 18.8%     | 0.42               | 15.4%                    | 14.3%     | 0.58               |
| Percent employed at random assignment | 20.7%                  | 29.2%     | 0.11               | 16.3%                    | 18.2%     | 0.54               | 18.1%                 | 20.6%     | 0.36               | 16.0%                    | 17.8%     | 0.38               |
| Percent received AFDC at RA           | 14.3%                  | 20.2%     | 0.21               | 16.8%                    | 17.4%     | 0.85               | 63.4%                 | 59.6%     | 0.25               | 57.3%                    | 62.7%     | 0.05               |
|                                       | Male youth trainees    |           |                    |                          |           |                    | Female youth trainees |           |                    |                          |           |                    |
|                                       | Male youth nontrainees |           |                    | Female youth nontrainees |           |                    | Male youth trainees   |           |                    | Female youth nontrainees |           |                    |
|                                       | Treat-ments            | Con-trols | Prob ( $t >  T $ ) | Treat-ments              | Con-trols | Prob ( $t >  T $ ) | Treat-ments           | Con-trols | Prob ( $t >  T $ ) | Treat-ments              | Con-trols | Prob ( $t >  T $ ) |
| Sample size                           | 210                    | 60        |                    | 167                      | 114       |                    | 430                   | 141       |                    | 304                      | 211       |                    |
| Percent black                         | 22.4%                  | 26.7%     | 0.51               | 27.5%                    | 27.2%     | 0.95               | 24.2%                 | 24.8%     | 0.88               | 28.3%                    | 25.6%     | 0.50               |
| Percent Hispanic                      | 30.0%                  | 21.7%     | 0.18               | 21.6%                    | 24.6%     | 0.56               | 28.1%                 | 25.5%     | 0.54               | 17.1%                    | 24.6%     | 0.04               |
| Percent with 12 years schooling       | 41.4%                  | 41.7%     | 0.97               | 30.5%                    | 40.4%     | 0.09               | 49.3%                 | 56.7%     | 0.13               | 47.4%                    | 45.0%     | 0.60               |
| Percent with > 12 years schooling     | 6.2%                   | 11.7%     | 0.23               | 0.6%                     | 1.8%      | 0.40               | 4.7%                  | 9.2%      | 0.09               | 4.3%                     | 2.4%      | 0.22               |
| Percent employed at random assignment | 18.6%                  | 28.3%     | 0.13               | 18.6%                    | 17.5%     | 0.83               | 20.7%                 | 25.5%     | 0.25               | 16.4%                    | 21.8%     | 0.13               |
| Percent received AFDC at RA           | 16.2%                  | 16.7%     | 0.93               | 13.8%                    | 8.8%      | 0.19               | 45.1%                 | 42.6%     | 0.60               | 38.2%                    | 39.3%     | 0.79               |

The sample is rectangular and includes all persons from the sixteen experimental sites, recommended to receive classroom training,  $T$ -tests are of the null hypothesis that means of the treatment, and control samples are equal within demographic and training groups.